

Linear Equations

An equation is an open sentence that states that two algebraic expressions are equal. An equation is **linear** if the variables on either side of the equal sign have a highest exponent value or degree of one.

We keep an equation in **balance** by performing **inverse operations** to both sides of an equation.

3 Types of Equations:

1. **Conditional:** an equation that is true for only some values of the variable. Ex: $8x = 16$ *1 solution*
2. **Identities:** an equation that is true for all values of the variables. Ex: $4x + 2x = 6x$ *∞ many*
3. **Contradiction:** When a determined value does not satisfy the equation (make it true) or when an equation ends up having no variables. Ex: $1 + x = x$
 $-x - x$
 $1 \neq 0$ *No solution*

Properties of Equality: WB pp. 46 and 48

In the given solution, state the property being used:

$$(a + 8) - 5 = 17$$

Given

$$a + (8 - 5) = 17$$

associative property

$$a + 3 = 17$$

Simplify

$$a + 3 - 3 = 17 - 3$$

subtraction property of equality

$$a + 0 = 17 - 3$$

additive inverse

$$a = 17 - 3$$

additive identity

$$a = 14$$

Simplify

Simplify $2(4 + 1) - 8x$ and name the property that justifies each step.

$2(4x + 1) - 8x$	Given
$(8x + 2) - 8x$	Distributive Property
$(2 + 8x) - 8x$	Commutative Property of Addition
$2 + (8x - 8x)$	Associative Property
$2 + 0$	Additive Inverse
2	Additive Identity

Classwork: WB pp. 47 - 51

HW: WB p. 48 #s 9, 10, 19 -23 and p. 51 #s 14 - 22

Math & HW: p125
 p129 #s 1-8 odd
 due Fri

Pythagorean Theorem

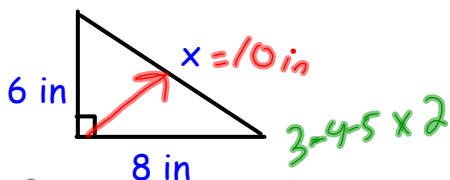
$$a^2 + b^2 = c^2$$

a and b represent the legs of a right triangle

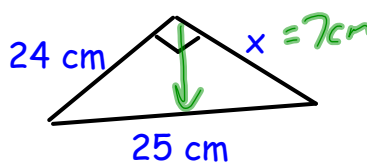
and c represent the hypotenuse

↳ across from the right angle
 largest side

Find the length of the missing side:

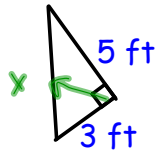


$$\begin{aligned}
 a^2 + b^2 &= c^2 \\
 6^2 + 8^2 &= x^2 \\
 36 + 64 &= x^2 \\
 \sqrt{100} &= \sqrt{x^2} \\
 10 &= x
 \end{aligned}$$



$$\begin{aligned}
 a^2 + b^2 &= c^2 \\
 24^2 + x^2 &= 25^2 \\
 576 + x^2 &= 625 \\
 -576 & \quad -576 \\
 \hline
 x^2 &= 49 \\
 \sqrt{x^2} &= \sqrt{49} \\
 x &= 7
 \end{aligned}$$

Find the length of the missing sides:



$$a^2 + b^2 = c^2$$

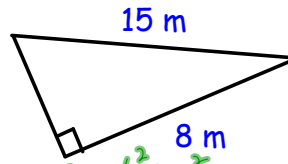
$$3^2 + 5^2 = x^2$$

$$9 + 25 = x^2$$

$$\sqrt{34} = \sqrt{x^2}$$

$$x = \sqrt{34} \approx 5.8$$

$5^2 = 25$
 $6^2 = 36$



$$a^2 + b^2 = c^2$$

$$8^2 + x^2 = 15^2$$

$$64 + x^2 = 225$$

$$-64 \quad -64$$

$$\sqrt{x^2} = \sqrt{161}$$

$$x = \sqrt{161} \approx 12.7$$

$12^2 = 144$
 $13^2 = 169$



Pythagorean Triples (Triplets)

The following triples, and any multiple, always make a right triangle.

3, 4, 5

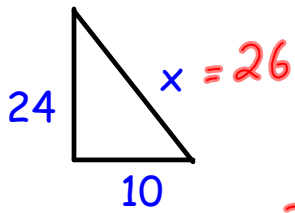
5, 12, 13

7, 24, 25

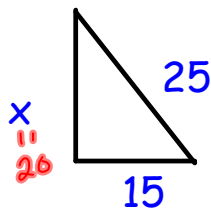
8, 15, 17

20, 21, 29

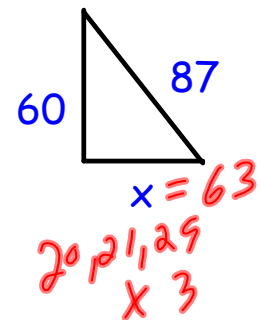
Find the missing length of the triangle:



$$5, 12, 13 \times 2$$



$$3, 4, 5 \times 5$$

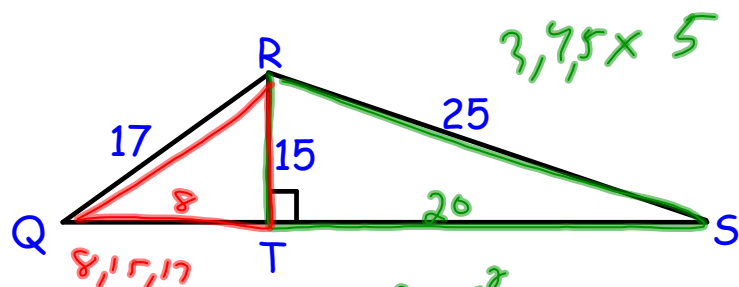


$$20, 21, 29 \times 3$$

Pythagorean Theorem Problems Day 2

Find the length of QS.

$$\overline{QS} = 28$$



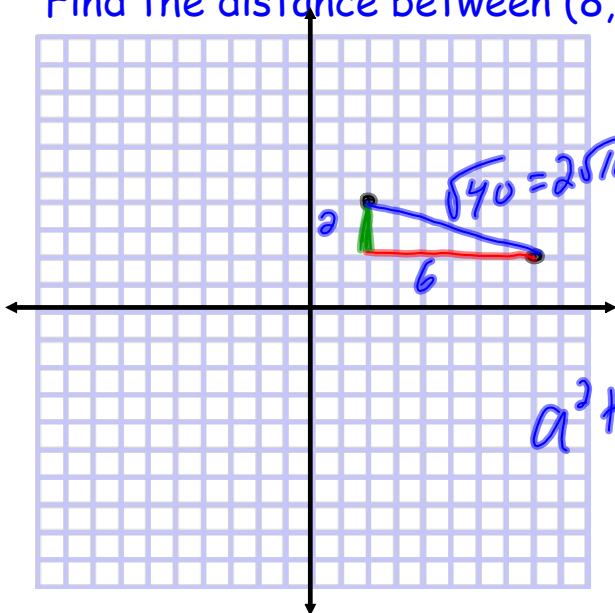
$$15^2 + x^2 = 25^2$$

$$225 + x^2 = 625$$

$$\sqrt{x^2} = \sqrt{400}$$

$$x = 20$$

Find the distance between $(8, 2)$ and $(2, 4)$.



$$a^2 + b^2 = c^2$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$(8-2)^2 \quad (2-4)^2$$

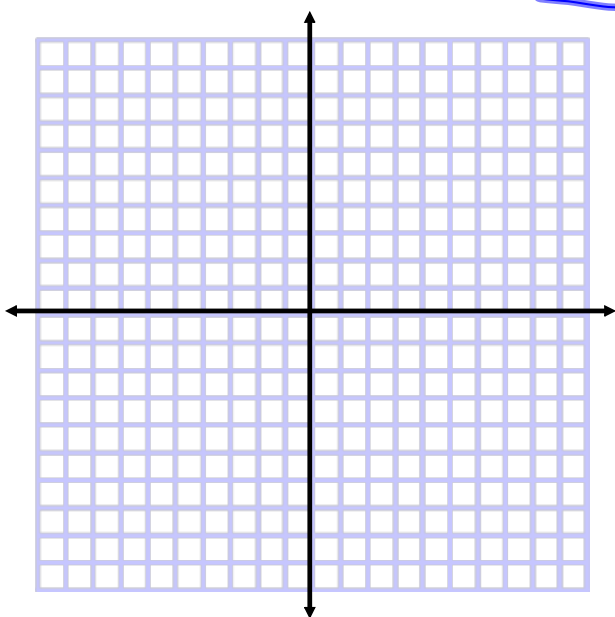
$$6^2 \quad (-2)^2$$

$$d = \sqrt{36 + 4}$$

$$\sqrt{40}$$

$$2\sqrt{10}$$

Find the distance between $(-5, -4)$ and $(-2, -1)$.



$$3^2 + 3^2 = c^2$$

$$9 + 9 = c^2$$

$$\sqrt{18} = \sqrt{c^2}$$

$$\sqrt{9} = \sqrt{9}$$

$$3 = 3$$

$$3\sqrt{2} = c$$

